



UNIVERSITY *of* LIMERICK
OLLSCOIL LUIMNIGH

Faculty of Science and Engineering
Department of Mathematics & Statistics

MID TERM ASSESSMENT PAPER

MODULE CODE: MA4003

SEMESTER: Autumn 2011/12

MODULE TITLE: Engineering Mathematics 3 DURATION OF EXAMINATION: 45 minutes

LECTURER: Dr. M. Burke

PERCENTAGE OF TOTAL MARKS: 20 %

Colour: Yellow

**INSTRUCTIONS TO CANDIDATES: Answer all questions. All questions carry equal marks.
Use the Answer Sheet below.**

ANSWER SHEET

STUDENT'S NAME:

STUDENT'S ID NUMBER:

For each question, place an "X" in the box of your choice.

Question	a	b	c	d	e	Do not write in this column
1					X	
2				X		
3	X					
4				X		
5			X			
6		X				
7	X					
8			X			
9		X				
10					X	

Table of Laplace Transforms

$f(t), t \geq 0$	$F(s) = \mathcal{L}[f(t)]$
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
t^n	$\frac{n!}{s^{n+1}}$
e^{at}	$\frac{1}{s-a}$
$t^n e^{at}$	$\frac{n!}{(s-a)^{n+1}}$
$\sinh at$	$\frac{a}{s^2-a^2}$
$\cosh at$	$\frac{s}{s^2-a^2}$
$\frac{1}{a-b}(e^{at} - e^{bt})$	$\frac{1}{(s-a)(s-b)}$
$\frac{a}{a-b}e^{at} - \frac{b}{a-b}e^{bt}$	$\frac{s}{(s-a)(s-b)}$
$\sin at$	$\frac{a}{s^2+a^2}$
$\cos at$	$\frac{s}{s^2+a^2}$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2F(s) - sf(0) - f'(0)$
$\int_0^t f(\tau) d\tau$	$\frac{1}{s}F(s)$
$e^{at}f(t)$	$F(s-a)$
Heaviside $u_a(t)$	$\frac{e^{-as}}{s}$
$f(t-a)u_a(t)$	$e^{-as}F(s)$
Ramp $R(t-a)$	$\frac{e^{-as}}{s^2}$
$tf(t)$	$-F'(s)$
$\frac{f(t)}{t}$	$\int_s^\infty F(\sigma) d\sigma$
$(f * g)(t) \equiv \int_0^t f(t-\tau)g(\tau) d\tau$	$F(s)G(s)$
$f(t) = f(t+p)$	$\frac{1}{1-e^{-sp}} \int_0^p f(t)e^{-st} dt$

All $f(t)$ are defined for $t \geq 0$.

1. The Laplace Transform of $\cos 3t - \sin 3t$ is

(a) $\frac{s-3}{(s^2+9)^2}$ (b) $\frac{1}{s-3}$ (c) $\frac{1}{s}$ (d) $\frac{1}{s+3}$ (e) $\frac{s-3}{s^2+9}$

2. The Laplace Transform of $e^{4t}(5t-1)$ is

(a) $\frac{5s-1}{(s-4)^2}$ (b) $\frac{5-s}{s^2(s-4)}$ (c) $\frac{5}{s^2-16}$ (d) $\frac{9-s}{(s-4)^2}$ (e) $\frac{5s-1}{(s+4)^2}$

3. The Laplace Transform of $f(t) = \sin(2t-6)u_3(t)$ is

(a) $\frac{2}{s^2+4}e^{-3s}$ (b) $\frac{2e^{-3}}{s(s^2+4)}$ (c) $\frac{3}{s^2+9}e^{-2s}$ (d) $\frac{s}{s^2+9}e^{-3s}$ (e) $\frac{3}{s^2+4}e^{-s}$

4. The inverse Laplace transform of $\frac{1}{s^2}e^{-2s}$ is

(a) te^{-2t} (b) te^t (c) $tu_2(t)$ (d) $(t-2)u_2(t)$ (e) $(t-2)e^{-t}$

5. The inverse Laplace transform of $\frac{s-1}{s^2-2s+2}$ is

(a) e^{-2t} (b) $\frac{1}{3}e^{2t} + \frac{2}{3}e^{-t}$ (c) $e^t \cos t$ (d) $e^t \cos 2t$ (e) e^{2t}

6. The convolution of t^2 with t^2 (also denoted by $t^2 * t^2$) is given by

(a) $\frac{t^6}{720}$ (b) $\frac{t^5}{30}$ (c) $\frac{t^4}{4}$ (d) $\frac{t^4}{6}$ (e) $\frac{t^2}{2}$

7. The function $f: \mathbb{R} \rightarrow \mathbb{R}$ satisfies $f(x+2\pi) = f(x)$. The period of $f(2x)$ is

(a) π (b) 2 (c) 2π (d) 4 (e) 4π

8. The functions $f(x) = x - x^5$ and $g(x) = x \sin x$ defined on $-1 < x < 1$ have the property that

- (a) both are even (b) both are odd (c) f is odd and g is even
(d) f is even and g is odd (e) at least one is neither even nor odd

9. The function $f(x) = \begin{cases} 1, & \text{if } -1 < x < 0 \\ -1, & \text{if } 0 < x < 1 \end{cases}$ is periodic with period 2.

It has a Fourier Series $\sum_{n=1}^{\infty} b_n \sin(n\pi x)$; b_3 is given by

(a) $-\frac{2}{3}$ (b) $-\frac{4}{3\pi}$ (c) 0 (d) $\frac{4}{3\pi}$ (e) $\frac{2}{3}$

10. The coefficient a_0 in the Fourier Series for the periodic function $f(x) = \cosh x$ if $-1 < x < 1$ with period 2 has the value

(a) $-2 \cosh 1$ (b) $-\sinh 1$ (c) 0 (d) $\cosh 1$ (e) $2 \sinh 1$